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Near-infrared laser pumped intersubband THz laser gain in InGaAs-AIAsSb-InP quantum wells

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We investigate the possibility of using InGaAs–AlAsSb–InP coupled quantum wells to generate THz radiation by means of intersubband optical pumping. We show that large conduction band offsets of these quantum wells make it possible to use conventional near-infrared diode lasers around 1.55 μ m as pump sources. Taking into account the pump–probe coherent interaction and the optical nonlinearity for the pump field, we calculate the THz gain of the quantum well structure. We show that resonant Raman scattering enhances the THz gain at low and moderate optical pumping levels. When the pump intensity is strong, the THz gain is reduced by pump-induced population redistribution and pump–probe coherent interactions. © 2000 American Institute of Physics. [S0003-6951(00)02015-5]

The early proposal¹ and recent demonstration² of intersubband semiconductor quantum well (QW) lasers have aroused considerable interest because of their potential applications in the midinfrared frequency range and because only electrons participate in the lasing process, which is different from the conventional semiconductor lasers based on interband transitions. Up to now, the electrically injected quantum cascade lasers have been very successful in the midinfrared range.^{3,4} The optically pumped intersubband lasers have also been demonstrated in the wavelength around 15 μm.^{5,6} A natural question is whether the concept of the intersubband laser can be generalized to much longer wavelength preferably to 30–300 μ m or THz range. ^{7–9} This question is especially interesting due to the current lack of solidstate THz sources and the enormous potential applications of such sources. Compared to the electrically injected lasers, the optically pumped lasers have advantages of easier realization of population inversion and less sophisticated device design. In addition, in the optical pumping case, not only the pumpinduced population inversion gives rise to the optical gain, but the resonant Raman process in the quantum well also contributes to the gain. 10,11 This gain enhancement due to the Raman processes relaxes the requirement of population inversion, which is more difficult to achieve in the THz frequency range.

Previously, the optically pumped intersubband lasers were made of GaAs/AlGaAs quantum wells.^{5,6} Since the conduction band offset of these quantum wells are usually small (~300 meV), CO₂ lasers were employed as pump sources.^{5,6,8} Therefore, it is almost impossible to build a compact THz system based on CO₂ laser pumping. In this letter, we propose to use optically pumped InGaAs–AlAsSb–InP coupled quantum wells to generate THz radiation. The advantage of our quantum well design is that the large band edge offset allows the conventional diode laser to be used as a pump source and that the pump laser and THz laser may be integrated eventually monolithically or by het-

erogeneous bonding. Owing to the large conduction band offset, the near-infrared intersubband transitions in InGaAs–AlAsSb double quantum wells have been recently demonstrated.¹²

We design a four-subband ($E_1 - E_4$) THz laser consisting of a lattice-matched $In_{0.53}Ga_{0.47}As/AlAs_{0.56}Sb_{0.44}/InP/AlAs_{0.56}Sb_{0.44}/InP$ triple quantum well embedded in AlAs_{0.56}Sb_{0.44} barrier materials, as shown in Fig. 1. (The four-level structures based on GaAs/AlGaAs triple¹³ and step¹⁴ quantum wells have been studied recently and shown to allow easier population inversion.) The quantum well structure is assumed to be modulation n-type doped and biased with a dc electric field. To obtain the eigenenergies and envelope wave functions of the QW, we solve the effective-mass Schrödinger equation coupled with Poisson equation. The exchange-correlation effect is included in the local-density approximation. The conduction band offsets between AlAs_{0.56}Sb_{0.44} and $In_{0.53}Ga_{0.47}As$ and between AlAs_{0.56}Sb_{0.44}

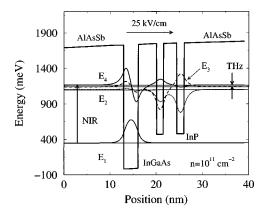


FIG. 1. Self-consistent potential and the four lowest energy levels with corresponding wave functions of an $\rm In_{0.53}Ga_{0.47}As/AlAs_{0.56}Sb_{0.44}/InP$ AlAs_0.56Sb_0.44/InP triple quantum well structure biased with a dc electric field of 25 kV/cm. $\rm In_{0.53}Ga_{0.47}As$ well width is 3.1 nm and InP well width is 1.5 nm. The thicknesses of the wider and narrower barrier layers are 4.0 and 2.9 nm, respectively. The calculated transition energies (E_{ij}) and dipole matrix elements (Z_{ij}) are $E_{43}\!=\!21.2$ meV, $E_{32}\!=\!42.1$ meV, $E_{41}\!=\!810$ meV, $Z_{21}\!=\!0.4$ Å, $Z_{31}\!=\!2.3$ Å, $Z_{41}\!=\!8.5$ Å, $Z_{32}\!=\!18.7$ Å, $Z_{42}\!=\!1.1$ Å, and $Z_{43}\!=\!17.6$ Å.

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and InP are 1.7^{12} and 1.376 eV, respectively. The conduction band nonparabolicity is taken into account in the energy-dependent effective-mass scheme.¹⁵ For a sheet concentration of $n = 10^{11}$ cm⁻², the calculated self-consistent potential, the four energy levels, and the corresponding wave functions are shown in Fig. 1.

Let us now consider the situation where the quantum well is subjected to a pump field of angular frequency ω_n and a weak signal field of frequency ω . The polarizations of both pump (E_p) and probe (E_{ω}) fields are assumed to be along the well growth direction (z axis). The pump photon energy is close to the energy spacing E_{41} between the ground state and the highest lying subband, while the probe photon energy is in the vicinity of the subband separation E_{43} . In this case, both pump and probe fields do not resonantly couple subband E_2 . Thus, we will not include polarizations involving this subband in the calculation of the pump-probe coherence for simplicity. However, we incorporate it into the calculation of the population distribution because its presence allows the electrons in subband E_3 to relax fast into subband E_2 through emission of longitudinal-optical (LO) phonons and these electrons finally jump to the ground state. To describe the probe field response of the quantum well system in the presence of a strong pump field, we start with the single-particle density-matrix formalism. Under the rotating-wave approximation (RWA), we obtain the following coupled equations for the steady-state electron distribution function (f_i) and the polarization (ρ_{ij}) between subbands i and j (for brevity, we drop the electron wave-vector index in our notation):^{11,16}

$$2\operatorname{Im}[\Omega_{31}^*(\omega_p)\rho_{31}(\omega_p) + \Omega_{41}^*(\omega_p)\rho_{41}(\omega_p)]$$

$$-\frac{f_1 - f_1^F}{T_{cc}} + \frac{f_2}{\tau_{21}} + \frac{f_3}{\tau_{31}} + \frac{f_4}{\tau_{41}} = 0,$$
 (1)

$$-\frac{f_2 - f_2^F}{T_{cc}} + \frac{f_3}{\tau_{32}} + \frac{f_4}{\tau_{42}} - \frac{f_2}{\tau_{21}} = 0, \tag{2}$$

$$-2\operatorname{Im}[\Omega_{31}^{*}(\omega_{p})\rho_{31}(\omega_{p})] - \frac{f_{3} - f_{3}^{F}}{T_{cc}} + \frac{f_{4}}{\tau_{43}} - \frac{f_{3}}{\tau_{32}} - \frac{f_{3}}{\tau_{31}} = 0,$$
(3)

$$-2\operatorname{Im}\left[\Omega_{41}^{*}(\omega_{p})\rho_{41}(\omega_{p})\right] - \frac{f_{4} - f_{4}^{F}}{T_{cc}} - \frac{f_{4}}{\tau_{43}} - \frac{f_{4}}{\tau_{42}} - \frac{f_{4}}{\tau_{41}} = 0, (4)$$

 $D_{43}(\omega)\rho_{43}(\omega)$

$$= (f_3 - f_4)\Omega_{43}(\omega) + \rho_{13}(\omega - \omega_p)\Omega_{41}(\omega_p)$$
$$-\rho_{41}(\omega + \omega_p)\Omega_{31}^*(\omega_p), \tag{5}$$

$$D_{13}(\omega-\omega_p)\rho_{13}(\omega-\omega_p)$$

$$= \rho_{43}(\omega)\Omega_{41}^*(\omega_p) - \rho_{41}^*(\omega_p)\Omega_{43}(\omega), \tag{6}$$

$$D_{41}(\omega + \omega_n)\rho_{41}(\omega + \omega_n)$$

$$= -\rho_{43}(\omega)\Omega_{31}(\omega_p) + \rho_{31}(\omega_p)\Omega_{43}(\omega), \tag{7}$$

$$D_{31}(\omega_p)\rho_{31}(\omega_p) = (f_1 - f_3)\Omega_{31}(\omega_p) - \rho_{43}^*(0)\Omega_{41}(\omega_p), \quad (8)$$

$$D_{41}(\omega_p)\rho_{41}(\omega_p) = (f_1 - f_4)\Omega_{41}(\omega_p) - \rho_{43}(0)\Omega_{31}(\omega_p), \quad (9)$$

$$D_{43}(0)\rho_{43}(0) = \rho_{31}^*(\omega_p)\Omega_{41}(\omega_p) - \rho_{41}(\omega_p)\Omega_{31}^*(\omega_p). \tag{10}$$

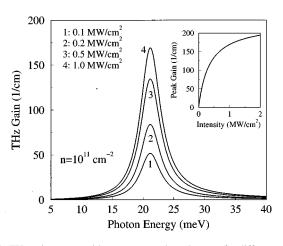


FIG. 2. THz gain spectra without pump-probe coherence for different pump intensities. The maximum gain as a function of the pump intensity is shown in the inset.

In Eqs. (5)–(10), only resonant terms are considered. Also, the optical nonlinearity for the pump field is included. That effect was neglected in our previous work. 11 $\Omega_{ij}(\omega,\omega_p)=(E_\omega,E_p)\mu_{ij}/\hbar$, $D_{ij}(\omega)=\omega+i\gamma_{ij}-E_{ij}/\hbar$; γ_{ij} is the line broadening factor and μ_{ij} is the dipole moment. T_{cc} and τ_{ij} are the intrasubband carrier–carrier scattering and intersubband relaxation times, respectively. The quantity f_i^F denotes the Fermi–Dirac distribution function of the QW without the pump light. It is easy to see from Eqs. (1)–(4) that the pump field induces an electron population redistribution that is coupled with the intersubband polarization. Thus, by solving Eqs. (1)–(10), we simultaneously obtain the electron distribution function as well as the off-diagonal element $\rho_{43}(\omega)$, which determines the optical gain of the THz probe field. Then we can calculate the THz gain following Ref. 11.

For the QW structure given in Fig. 1, we performed numerical studies of the THz gain spectra. In our calculations, the following parameters were used: $T_{cc} = 0.3$, $\tau_{21} = 1.5$, $\tau_{31} = 1.0$, $\tau_{41} = 1.2$, $\tau_{32} = 0.4$, $\tau_{42} = 1.0$, and $\tau_{43} = 1.5$ ps. ^{5,14} Note that the ratio τ_{43}/τ_{32} is about 4, which is consistent with the calculations. ¹⁷ Among these lifetimes, it is the ratio τ_{43}/τ_{32} that affects mostly the THz gain due to the population inversion. The line broadening factors are $\hbar \gamma_{43} = 2.0$ meV and $\hbar \gamma_{41} = \hbar \gamma_{31} = 3.0$ meV. The temperature is 77 K. Here we should mention that the electron density of 10^{11} cm⁻² used in Fig. 1 will introduce a "moderately strong" free-carrier plasma absorption in the THz range.

To understand the role of the pump-probe coherence in the probe response of the QW, we show in Fig. 2 the THz gain spectra at different pump intensities obtained by neglecting pump-probe coherent interactions. Namely, the calculated optical gain in Fig. 2 results purely from the pump-induced population inversion. The pump photon energy used in Fig. 2 is $\hbar \omega_p = E_{41} = 0.81 \,\text{eV}$ (1.53 μ m) that is close to the wavelength of the conventional communication lasers. We see from Fig. 2 that the THz gain increases as the pump intensity is increased, and the peak gain appears at the probe photon energy equal to the transition energy E_{43} . It is also evident that the increase in the maximum gain becomes slower when the pump intensity becomes larger (see the inset of Fig. 2). This gain saturation behavior is a direct result of population inversion saturation at high pump intensities, as

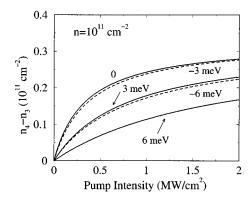


FIG. 3. Population difference vs the pump intensity at different pump detunings, i.e., $\hbar \omega_p - E_{41} = -6$, -3, 0, 3, and 6 meV.

illustrated in Fig. 3. Note that there is an obvious difference in the pump intensity dependence of the population inversion for positive and negative pump detunings as shown in Fig. 3. This is due mainly to the band nonparabolicity effect that effectively reduces the intersubband separation at nonzero wave vectors. The saturation behavior of the population inversion is pump frequency dependent.

In Fig. 4 we show the THz gain spectra for different pump intensities calculated with the pump-probe coherence included. As in Fig. 2, the pump photon energy is $\hbar \omega_p = E_{41}$. Comparing Figs. 2 and 4 we see that, for small pump intensities (say less than 0.2 MW/cm²), the coherent pump-probe interaction enhances the THz gain. This is so because in the pump-probe scheme considered in this letter, the resonant Raman scattering in the QW gives rise to a Raman gain in addition to the gain due to the population inversion. Thus one would expect that the THz gain increases with an increase in the pump intensity because the Raman gain is increased as well. However, we see from Fig. 4 that the peak THz gain first increases and then decreases when the pump intensity is increased. As the pump intensity is furtherly in-

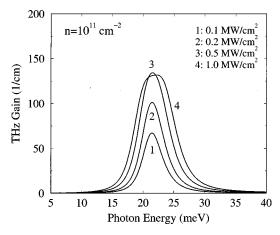


FIG. 4. THz gain spectra with pump-probe coherence for different pump intensities.

creased, the gain approaches to a constant value. We also see from Fig. 4 that the peak location in the gain spectra is blue-shifted with increasing the pump intensity, which is not shown in Fig. 2. This is because of the pump-probe interaction induced shift effect that is neglected in Fig. 2.

In summary, we have proposed to use a near-infrared pumped InGaAs-AlAsSb-InP triple quantum well to obtain THz gain. Owing to the large conduction band offset of the QW structure, we show that the THz radiation can be generated with a near-infrared diode lasers around 1.55 µm. We optimized the QW design to enhance the pump-induced population inversion between the two lasing subbands by adding a subband with an energy separation to the lower lasing subband close to the LO phonon energy. The THz gain is calculated by including the pump-probe coherent interaction. We showed that resonant Raman scattering enhances the THz gain at low and moderate pump intensities. At the high pumping level, the THz gain becomes smaller because of pump-induced population redistribution and pump-probe coherent interactions. We finally stress that the THz devices proposed in this letter combine the following major advantages in a single design: optical coherent gain enhancement, maximized inversion due to the phonon resonant depopulation, and the near-infrared pumping. We hope this would lead us a step further in our efforts to realize a THz laser based on QW-intersubband transitions.

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- ¹R. F. Kazarinov and R. A. Suris, Sov. Phys. Semicond. 5, 172 (1971).
- ²J. Faist, F. Capasso, D. Sivco, C. Sirtori, A. L. Hutchinson, S. N. G. Chu, and A. Y. Cho, Science 264, 553 (1994).
- ³J. Faist, F. Capasso, D. Sivco, C. Sirtori, J. N. Baillargeon, A. L. Hutchinson, S. N. G. Chu, and A. Y. Cho, Appl. Phys. Lett. 68, 3680 (1996).
- ⁴C. Sirtori, J. Faist, F. Capasso, D. Sivco, A. L. Hutchinson, and A. Y. Cho, Appl. Phys. Lett. **69**, 2810 (1996).
- ⁵O. Gauthier-Lafaye, P. Boucaud, F. H. Julien, S. Sauvage, S. Cabaret, J.-M. Lourtioz, V. Thierry-Mieg, and R. Planel, Appl. Phys. Lett. **71**, 3619 (1997).
- ⁶O. Gauthier-Lafaye, F. H. Julien, S. Cabaret, J.-M. Lourtioz, G. Strasser, E. Gornik, M. Helm, and P. Bois, Appl. Phys. Lett. **74**, 1537 (1999).
- ⁷B. Xu, Q. Hu, and M. R. Melloch, Appl. Phys. Lett. **71**, 440 (1997).
- ⁸I. Lyubomirsky, Q. Hu, and M. R. Melloch, Appl. Phys. Lett. **73**, 3043 (1998).
- ⁹M. Rochat, J. Faist, M. Beck, U. Oesterle, and M. Illegems, Appl. Phys. Lett. 73, 3724 (1998).
- ¹⁰ J. B. Khurgin, G. Sun, L. R. Friedman, and R. A. Soref, J. Appl. Phys. 78, 7398 (1995).
- ¹¹ A. Liu and C. Z. Ning, Appl. Phys. Lett. **75**, 1207 (1999).
- ¹² A. Neogi, T. Mozume, H. Yoshida, and O. Wada, IEEE Photonics Technol. Lett. 11, 633 (1999).
- ¹³I. Lyubomirsky and Q. Hu, Appl. Phys. Lett. **73**, 300 (1998).
- ¹⁴P. Kinsler, P. Harrison, and R. W. Kelsall, J. Appl. Phys. 85, 23 (1999).
- ¹⁵ D. F. Nelson, R. C. Miller, and D. A. Kleinman, Phys. Rev. B 35, 7770 (1987).
- ¹⁶ A. Liu, J. Opt. Soc. Am. B **15**, 1741 (1998).
- ¹⁷P. Harrison, R. W. Kelsall, P. Kinsler, and K. Donovan, in *IEEE Sixth International Conference on Terahertz Electronics Proceedings*, edited by P. Harrison, 1998 (unpublished), pp. 74–78.